CSE 5243 INTRO. TO DATA MINING

Data & Data Preprocessing Yu Su, CSE@The Ohio State University

Slides adapted from UIUC CS412 by Prof. Jiawei Han and OSU CSE5243 by Prof. Huan Sun

Data Preprocessing

- Data Preprocessing: An Overview
- Data Cleaning
- Data Integration

Summary

- Data Reduction and Transformation
- Dimensionality Reduction

Major tasks

Why Preprocess the Data? — Data Quality Issues

Measures for data quality: A multidimensional view

Accuracy: correct or wrong, accurate or not

Completeness: not recorded, unavailable, ...

Consistency: some modified but some not, dangling, ...

Timeliness: timely update?

Interpretability: how easily the data can be understood?

Trustworthiness: how trustable the data are correct?

What is Data Preprocessing? — Major Tasks

Data cleaning

Handle missing data, smooth noisy data,

identify or remove outliers, and resolve inconsistencies

Data integration

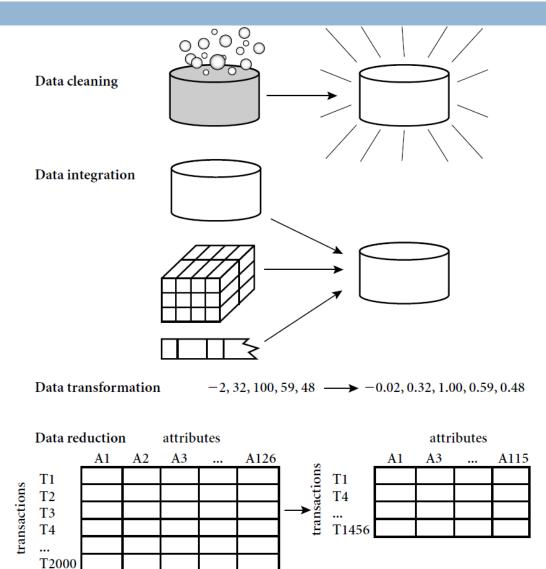
Integration of multiple databases, data cubes, or files

Data reduction

- Dimensionality reduction
- Numerosity reduction
- Data compression

Data transformation and data discretization

- Normalization
- Concept hierarchy generation



Chapter 3: Data Preprocessing

Data Preprocessing: An Overview



- Data Integration
- Data Reduction and Transformation
- Dimensionality Reduction
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Incomplete (Missing) Data

- Data is not always available
 - E.g., many tuples have no recorded value for several attributes, such as customer income in sales data
- Various reasons for missing:
 - Equipment malfunction
 - Inconsistent with other recorded data and thus deleted
 - Data were not entered due to misunderstanding
 - Certain data may not be considered important at the time of entry
 - Did not register history or changes of the data
- Missing data may need to be inferred

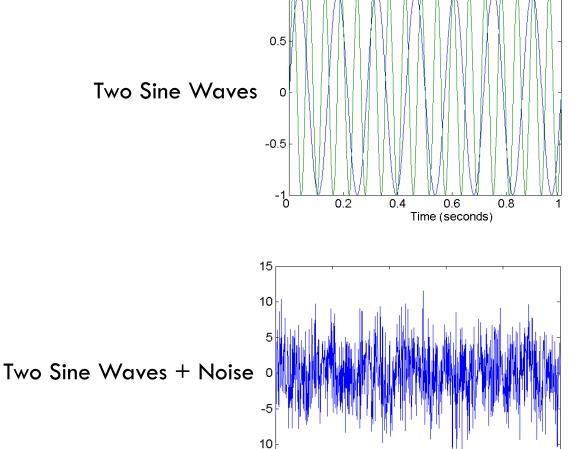
How to Handle Missing Data?

- Ignore the tuple: usually done when class label is missing (when doing classification) not effective when the % of missing values per attribute varies considerably
- □ Fill in the missing value manually: tedious + infeasible?
- □ Fill in it automatically with
 - a global constant : e.g., "unknown", a new class?!
 - the attribute mean
 - the attribute mean for all samples belonging to the same class: smarter
 - the most probable value: inference-based such as Bayesian formula or decision tree

Noisy Data

□ Noise: random error or variance in a measured variable

- Incorrect attribute values may be due to
 - Faulty data collection instruments
 - Data entry problems
 - Data transmission problems
 - Technology limitation
 - Inconsistency in naming convention
- Other data problems
 - Duplicate records
 - Inconsistent data



0.2

0.4

0.6 Time (seconds) 0.8

15 0

How to Handle Noisy Data?

Binning

- First sort data and partition into (equal-frequency) bins
- Then one can smooth by bin means, smooth by bin median, smooth by bin boundaries, etc.

Sorted data for *price* (in dollars): 4, 8, 15, 21, 21, 24, 25, 28, 34

Partiti	on into (equal-frequency) bins:		
Bin 1:	4, 8, 15		
Bin 2:	21, 21, 24		
Bin 3:	25, 28, 34		
Smoot	hing by bin means:		
Bin 1:	9, 9, 9		
Bin 2:	22, 22, 22		
Bin 3:	29, 29, 29		
Smoothing by bin boundaries:			
Bin 1:	4, 4, 15		
Bin 2:	21, 21, 24		
Bin 3:	25, 25, 34		

How to Handle Noisy Data?

Binning

- First sort data and partition into (equal-frequency) bins
- Then one can smooth by bin means, smooth by bin median, smooth by bin boundaries, etc.
- Regression
 - Smooth by fitting the data into regression functions
- Clustering
 - Detect and remove outliers
- Semi-supervised: Combined computer and human inspection
 - Detect suspicious values and check by human (e.g., deal with possible outliers)

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Data Integration

- Data integration
 - Combining data from multiple sources into a coherent store
- □ Schema integration: e.g., A.cust-id \equiv B.cust-#

Integrate metadata from different sources

- Entity identification:
 - Identify real world entities from multiple data sources, e.g., Bill Clinton = William Clinton
 - Often need domain knowledge or machine learning or both
- Detecting and resolving data value conflicts
 - **•** For the same real world entity, attribute values from different sources are different
 - Possible reasons: different representations, different scales, e.g., metric vs. British units
 - Need case-by-case analysis

Handling Redundancy in Data Integration

- Redundant data occur often when integration of multiple databases
 - Object identification: The same attribute or object may have different names in different databases
 - Derivable data: One attribute may be a "derived" attribute in another table, e.g., annual revenue

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 - Object identification: The same attribute or object may have different names in different databases
 - Derivable data: One attribute may be a "derived" attribute in another table, e.g., annual revenue
- Redundant attributes may be detected by correlation analysis and covariance analysis
- Careful integration of the data from multiple sources may help reduce/avoid redundancies and inconsistencies and improve mining speed and quality

$\Box \chi^2$ (chi-square) test:

To discover the correlation relationship between two nominal attributes, A and B.

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- Suppose <u>A</u> has <u>c</u> distinct values {<u>a1</u>, <u>a2</u>, ..., <u>ac</u>}, <u>B</u> has <u>r</u> distinct values {<u>b1</u>, <u>b2</u>, ..., <u>br</u>}.
- Contingency table: How many times the joint event (<u>Ai</u>, <u>Bi</u>), "attribute A takes on values ai and attribute B takes on value bj", happens based on the observed data tuples.

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$$\chi^2 = \sum_{i=1}^{c} \sum_{j=1}^{r} \frac{(o_{ij} - e_{ij})^2}{e_{ij}}$$

Where O_{ij} is the observed frequency (or, actual count) of the joint event (<u>Ai</u>, <u>Bi</u>), and O_{ij} is the expected frequency:

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- □ Note: Correlation does not imply causality
 - # of hospitals and # of car-theft in a city are correlated
 - Both are causally linked to the third variable: population

	Play chess	Not play chess	Sum (row)
Like science fiction	250 (90)	200 (360)	450
Not like science fiction	50 (210)	1000 (840)	1050
Sum (col.)	300	1200	1500

Contingency Table

Numbers outside bracket mean the observed frequencies of a joint event, and numbers inside bracket mean the expected frequencies.

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$\Box \chi^2$ (chi-square) calculation

 $\chi^{2} = \frac{\left(250 - 90\right)^{2}}{90} + \frac{\left(50 - 210\right)^{2}}{210} + \frac{\left(200 - 360\right)^{2}}{360} + \frac{\left(1000 - 840\right)^{2}}{840} = 507.93$

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How to derive 90? 450/1500 * 300 = 90

 $\Box \chi^2$ (chi-square) calculation (numbers in parenthesis are expected counts calculated based on the data distribution in the two categories)

$$\chi^{2} = \frac{(250 - 90)^{2}}{90} + \frac{(50 - 210)^{2}}{210} + \frac{(200 - 360)^{2}}{360} + \frac{(1000 - 840)^{2}}{840} = 507.93$$
Given a threshold 10.828

It shows that like_science_fiction and play_chess are correlated in the group

Review: Variance for Single Variable (Numerical Data)

The variance of a random variable X provides a measure of how much the value of X deviates from the mean or expected value of X:

$$\sigma^{2} = \operatorname{var}(X) = E[(X - \mu)^{2}] = \begin{cases} \sum_{x} (x - \mu)^{2} f(x) & \text{if } X \text{ is discrete} \\ \int_{-\infty}^{\infty} (x - \mu)^{2} f(x) dx & \text{if } X \text{ is continuous} \end{cases}$$

• where σ^2 is the variance of X, σ is called standard deviation $\mu = E[X]$ is the mean (or expected value) of X

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It can also be written as:

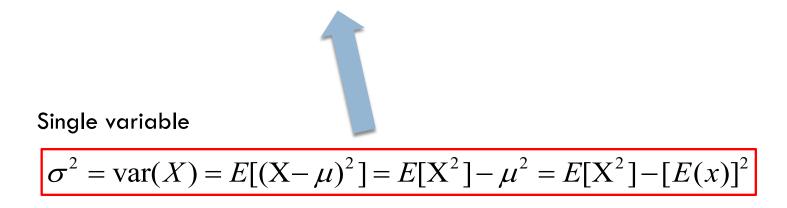
$$\sigma^{2} = \operatorname{var}(X) = E[(X - \mu)^{2}] = E[X^{2}] - \mu^{2} = E[X^{2}] - [E(X)]^{2}$$

Covariance for Two Variables

 \Box Covariance between two variables X_1 and X_2

$$\sigma_{12} = E[(X_1 - \mu_1)(X_2 - \mu_2)] = E[X_1 X_2] - \mu_1 \mu_2 = E[X_1 X_2] - E[X_1]E[X_2]$$

where $\mu_1 = E[X_1]$ is the mean (or expected value) of X_1 ; similarly for μ_2



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Sample covariance between X₁ and X₂:
$$\hat{\sigma}_{12} = \frac{1}{n} \sum_{i=1}^{n} (x_{i1} - \hat{\mu}_1)(x_{i2} - \hat{\mu}_2)$$

□ Sample covariance is a generalization of the sample variance:

$$\hat{\sigma}_{11} = \frac{1}{n} \sum_{i=1}^{n} (x_{i1} - \hat{\mu}_1)(x_{i1} - \hat{\mu}_1) = \frac{1}{n} \sum_{i=1}^{n} (x_{i1} - \hat{\mu}_1)^2 = \hat{\sigma}_1^2$$

For unbiased estimator, **n** => **n-1**

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- **Positive covariance:** If $\sigma_{12} > 0$
- □ Negative covariance: If $\sigma_{12} < 0$
- □ Independence: If X_1 and X_2 are independent, $\sigma_{12} = 0$, but the reverse is not true
 - Some pairs of random variables may have a covariance 0 but are not independent
 - Only under some additional assumptions (e.g., the data follow multivariate normal distributions) does a covariance of 0 imply independence

 \square Suppose two stocks X₁ and X₂ have the following values in one week:

- Day 1: (X₁, X₂) = (2, 5),
- Day 2: (X₁, X₂) = (3, 8),
- Day 3: (X₁, X₂) = (5, 10),
- Day 4: (X₁, X₂) = (4, 11),
- Day 5: (X₁, X₂) = (6, 14).

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Its computation can be simplified as:

E(X₁) = (2 + 3 + 5 + 4 + 6)/5 = 20/5 = 4

Example: Calculation of Covariance

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E(X₂) = (5 + 8 + 10 + 11 + 14) / 5 = 48 / 5 = 9.6

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$$\sigma_{12} = (2 \times 5 + 3 \times 8 + 5 \times 10 + 4 \times 11 + 6 \times 14)/5 - 4 \times 9.6 = 4$$

E[X1X2]

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 $\sigma_{12} = (2 \times 5 + 3 \times 8 + 5 \times 10 + 4 \times 11 + 6 \times 14)/5 - 4 \times 9.6 = 4$

□ Therefore, X_1 and X_2 rise together since $\sigma_{12} > 0$

Correlation Coefficient between Two Numerical Variables

Correlation between two variables X₁ and X₂ is the standard covariance, obtained by normalizing the covariance with the standard deviation of each variable

$$\rho_{12} = \frac{\sigma_{12}}{\sigma_1 \sigma_2} = \frac{\sigma_{12}}{\sqrt{\sigma_1^2 \sigma_2^2}}$$

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where n is the number of tuples, μ_1 and μ_2 are the respective means of X_1 and X_2 , σ_1 and σ_2 are the respective standard deviation of X_1 and X_2

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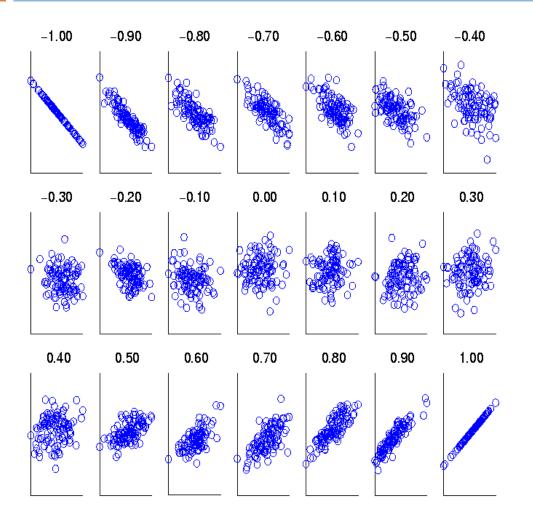
 \square If $\rho_{12} > 0$: A and B are positively correlated (X₁'s values increase as X₂'s)

The higher, the stronger correlation

 \Box If $\rho_{12} = 0$: independent (under the same assumption as discussed in co-variance)

□ If $\rho_{12} < 0$: negatively correlated

Visualizing Changes of Correlation Coefficient



□ Correlation coefficient value range: [-1, 1]

 A set of scatter plots shows sets of points and their correlation coefficients changing from – 1 to 1

Covariance Matrix

The variance and covariance information for variables X₁ and X₂ can be summarized as a 2 X 2 covariance matrix

$$\Sigma = E[(\mathbf{X} - \mu)(\mathbf{X} - \mu)^{T}] = E[\begin{pmatrix}X_{1} - \mu_{1}\\X_{2} - \mu_{2}\end{pmatrix}(X_{1} - \mu_{1} \quad X_{2} - \mu_{2})] = \begin{pmatrix}E[(X_{1} - \mu_{1})(X_{1} - \mu_{1})] & E[(X_{1} - \mu_{1})(X_{2} - \mu_{2})]\\E[(X_{2} - \mu_{2})(X_{1} - \mu_{1})] & E[(X_{2} - \mu_{2})(X_{2} - \mu_{2})]\end{pmatrix} = \begin{pmatrix}\sigma_{1}^{2} & \sigma_{12}\\\sigma_{21} & \sigma_{2}^{2}\end{pmatrix}$$

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$$D = \begin{pmatrix} x_{11} & x_{12} & \cdots & x_{1d} \\ x_{21} & x_{22} & \cdots & x_{2d} \\ \vdots & \vdots & \ddots & \vdots \\ x_{d1} & x_{d2} & \cdots & x_{dd} \end{pmatrix} \mathbf{\Sigma} = E[(\mathbf{X} - \mu)(\mathbf{X} - \mu)^T] = \begin{pmatrix} \sigma_1^2 & \sigma_{12} & \cdots & \sigma_{1d} \\ \sigma_{21} & \sigma_2^2 & \cdots & \sigma_{2d} \\ \vdots & \vdots & \ddots & \vdots \\ \sigma_{d1} & \sigma_{d2} & \cdots & \sigma_d^2 \end{pmatrix}$$

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Data Reduction

Data reduction:

Obtain a reduced representation of the data set

much smaller in volume but yet produces almost the same analytical results

□ Why data reduction?—A database/data warehouse may store terabytes of data

Complex analysis may take a very long time to run on the complete data set

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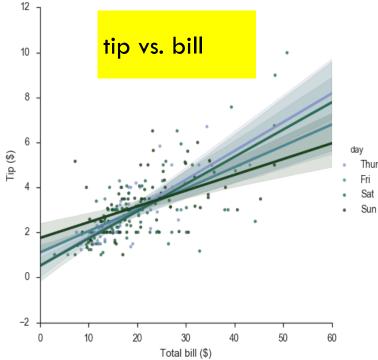
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- Why data reduction?—A database/data warehouse may store terabytes of data
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- **Methods for data reduction** (also data size reduction or numerosity reduction)
 - Regression and Log-Linear Models
 - Histograms, clustering, sampling
 - Data cube aggregation
 - Data compression

Data Reduction: Parametric vs. Non-Parametric Methods

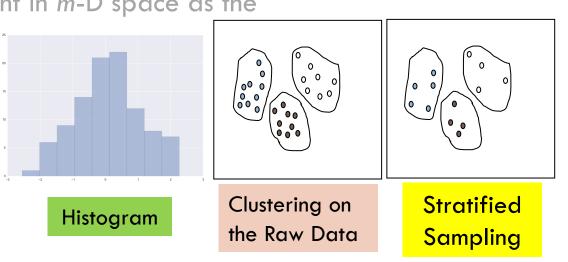
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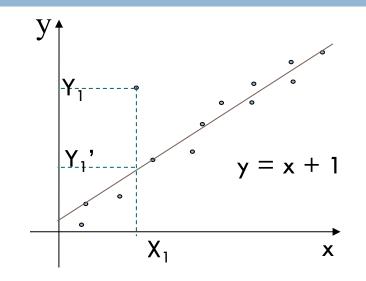
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- Parametric methods (e.g., regression)
 - Assume the data fits some model, estimate model parameters, store only the parameters, and discard the data (except possible outliers)
 - Ex.: Log-linear models—obtain value at a point in *m*-D space as the product on appropriate marginal subspaces
- Non-parametric methods
 - Do not assume models
 - Major families: histograms, clustering,

sampling, ...



 Regression analysis: A collective name for techniques for the modeling and analysis of numerical data consisting of values of a dependent variable (also called response variable or measurement) and of one or more independent variables (also known as explanatory variables or predictors)



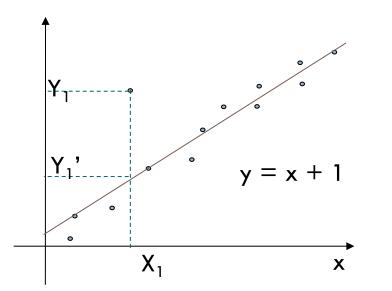
 Used for prediction (including forecasting of time-series data), inference, hypothesis testing, and modeling of causal relationships

Regression analysis:

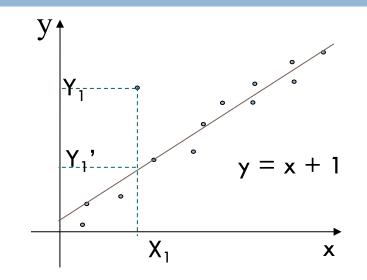
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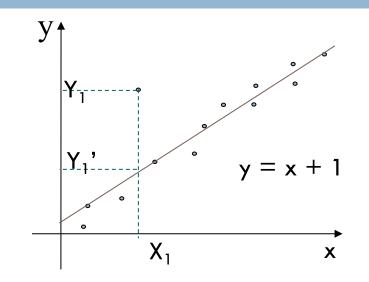
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- Most commonly the best fit is evaluated by using the *least squares method*, but other criteria have also been used



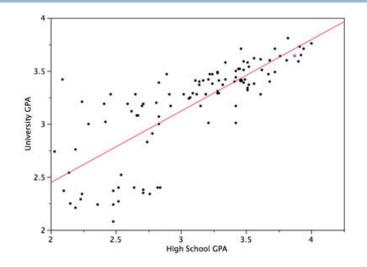
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Linear and Multiple Regression

- $\Box \ \underline{\text{Linear regression}}: Y = w X + b$
 - Data modeled to fit a straight line
 - Often uses the least-square method to fit the line
 - Two regression coefficients, w and b, specify the line and are to be estimated by using the data at hand
 - Using the least squares criterion to the known values of $(X_1, Y_1), (X_2, Y_2), ..., (X_n, Y_n)$

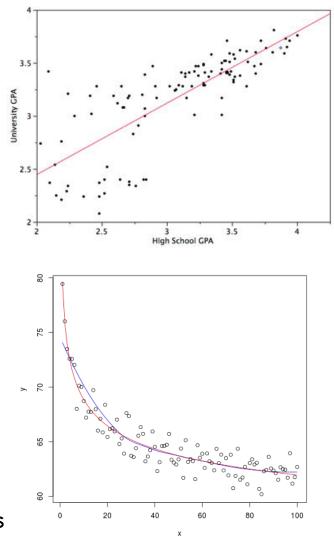


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□ <u>Nonlinear regression</u>:

- Data are modeled by a function which is a nonlinear combination of the model parameters and depends on one or more independent variables
- The data are fitted by a method of successive approximations

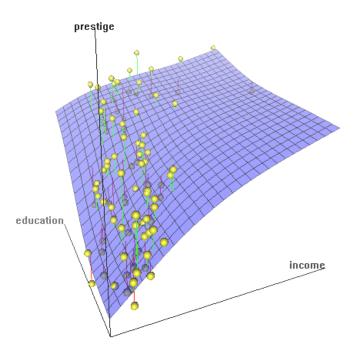


Multiple Regression

 $\square \quad \underline{\text{Multiple regression}}: Y = b_0 + b_1 X_1 + b_2 X_2$

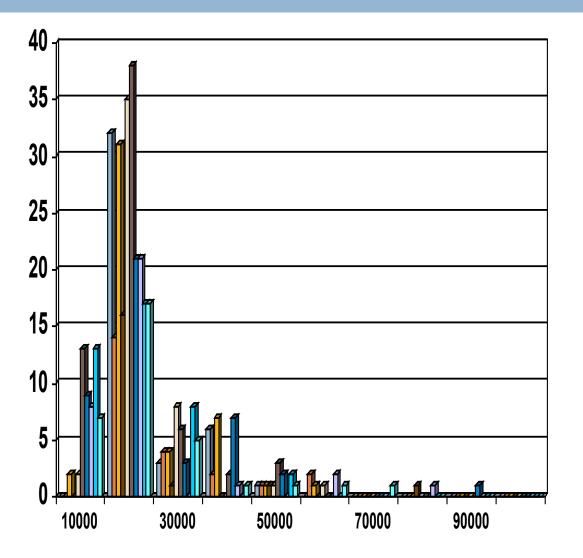
 Allows a response variable Y to be modeled as a linear function of multidimensional feature vector

Many nonlinear functions can be transformed into the above



Histogram Analysis

- Divide data into buckets and store average (sum) for each bucket
- Partitioning rules:
 - Equal-width: equal bucket range
 - Equal-frequency (or equal-depth)

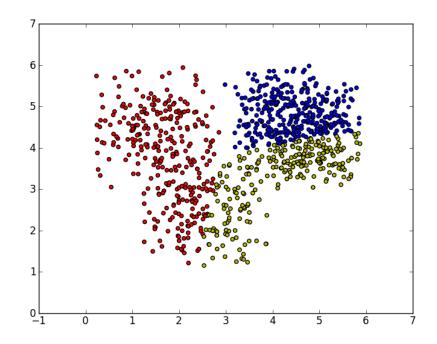


Clustering

Partition data set into clusters based on similarity,

and store cluster representation (e.g., centroid and diameter) only

- Can be very effective if data is clustered but not if data is "smeared"
- Can have hierarchical clustering and be stored in multi-dimensional index tree structures
- There are many choices of clustering definitions and clustering algorithms
- Cluster analysis will be studied in later this semester

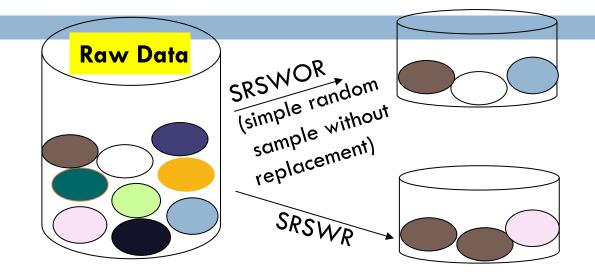


Sampling

- \Box Sampling: obtaining a small sample s to represent the whole data set N
- Allow a mining algorithm to run in complexity that is potentially sub-linear to the size of the data
- Key principle: Choose a representative subset of the data
 - Simple random sampling may have very poor performance in the presence of skew
 - Develop adaptive sampling methods, e.g., stratified sampling:

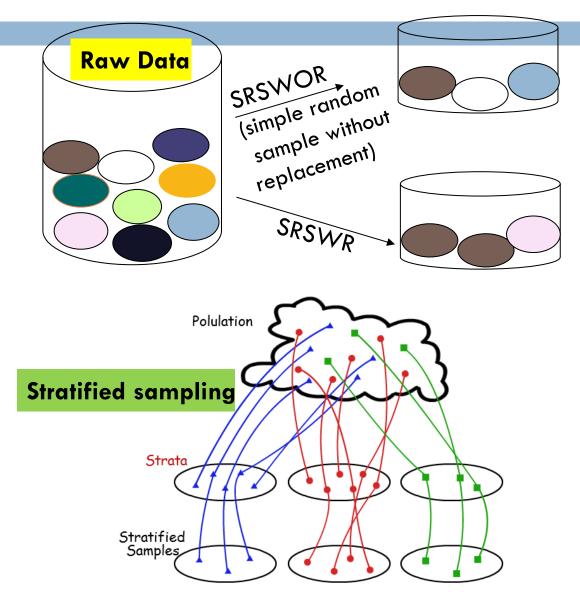
Types of Sampling

- Simple random sampling: equal probability of selecting any particular item
- Sampling without replacement
 - Once an object is selected, it is removed from the population
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Types of Sampling

- Simple random sampling: equal probability of selecting any particular item
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 - Once an object is selected, it is removed from the population
- Sampling with replacement
 - A selected object is not removed from the population
- Stratified sampling
 - Partition (or cluster) the data set, and draw samples from each partition (proportionally, i.e., approximately the same percentage of the data)



Chapter 3: Data Preprocessing

- Data Preprocessing: An Overview
- Data Cleaning
- Data Integration

Data Reduction and Transformation

Dimensionality Reduction

Summary

Data Transformation

A function that maps the entire set of values of a given attribute to a new set of replacement values s.t. each old value can be identified with one of the new values

Data Transformation

- A function that maps the entire set of values of a given attribute to a new set of replacement values s.t. each old value can be identified with one of the new values
- Methods
 - Smoothing: Remove noise from data
 - Attribute/feature construction
 - New attributes constructed from the given ones
 - Aggregation: Summarization, data cube construction
 - Normalization: Scaled to fall within a smaller, specified range
 - min-max normalization; z-score normalization; normalization by decimal scaling
 - Discretization: Concept hierarchy climbing

Normalization

□ **Min-max normalization**: to [new_min_A, new_max_A]

$$v' = \frac{v - min_A}{max_A - min_A} (new_max_A - new_min_A) + new_min_A$$

Ex. Let income range \$12,000 to \$98,000 normalized to [0.0, 1.0]

Then \$73,600 is mapped to
$$\frac{73,600-12,000}{98,000-12,000}(1.0-0)+0=0.716$$

- What if there's an outlier (e.g., 99 points in [0,40] and 1 point = 100)?
- What problem may be encountered when the transformation is applied to new data?

Normalization

□ **Min-max normalization**: to [new_min_A, new_max_A]

$$v' = \frac{v - min_A}{max_A - min_A} (new_max_A - new_min_A) + new_min_A$$

Z-score normalization (μ : mean, σ : standard deviation):

$$v' = \frac{v - \mu_A}{\sigma_A}$$

Z-score: The distance between the raw score and the population mean in the unit of the standard deviation

• Ex. Let $\mu = 54,000$, $\sigma = 16,000$. Then,

$$\frac{73,600-54,000}{16,000} = 1.225$$

Normalization

□ **Min-max normalization**: to [new_min_A, new_max_A]

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Normalization by decimal scaling

 $v' = v/10^{j}$, Where *j* is the smallest integer such that Max(|v'|) < 1

Discretization

Three types of attributes

- Nominal—values from an unordered set, e.g., color, profession
- Ordinal—values from an ordered set, e.g., military or academic rank
- Numeric—real numbers, e.g., integer or real numbers

Discretization: Divide the range of a continuous attribute into intervals

- Interval labels can then be used to replace actual data values
- Reduce data size by discretization
- Supervised vs. unsupervised
- Split (top-down) vs. merge (bottom-up)
- Discretization can be performed recursively on an attribute
- Prepare for further analysis, e.g., classification

Data Discretization Methods

□ Binning

- Top-down split, unsupervised
- Histogram analysis
 - Top-down split, unsupervised
- Clustering analysis
 - Unsupervised, top-down split or bottom-up merge
- Decision-tree analysis
 - Supervised, top-down split
- **Correlation (e.g.,** χ^2) analysis
 - Unsupervised, bottom-up merge
- □ Note: All the methods can be applied recursively

Simple Discretization: Binning

Equal-width (distance) partitioning

- Divides the range into N intervals of equal size: uniform grid
- □ if A and B are the lowest and highest values of the attribute, the width of intervals will be: W = (B A)/N.
- The most straightforward, but outliers may dominate presentation
- Skewed data is not handled well

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Equal-depth (frequency) partitioning

- Divides the range into N intervals, each containing approximately same number of samples
- Good data scaling
- Managing categorical attributes can be tricky

Example: Binning Methods for Data Smoothing

- □ Sorted data for price (in dollars): 4, 8, 9, 15, 21, 21, 24, 25, 26, 28, 29, 34
- Partition into equal-frequency (equi-width) bins:
 - Bin 1: 4, 8, 9, 15
 - Bin 2: 21, 21, 24, 25
 - Bin 3: 26, 28, 29, 34
- Smoothing by **bin means**:
 - Bin 1: 9, 9, 9, 9
 - Bin 2: 23, 23, 23, 23
 - Bin 3: 29, 29, 29, 29
- Smoothing by **bin boundaries**:
 - Bin 1: 4, 4, 4, 15
 - Bin 2: 21, 21, 25, 25
 - Bin 3: 26, 26, 26, 34

Discretization by Classification & Correlation Analysis

Classification (e.g., decision tree analysis)

- Supervised: Given class labels, e.g., cancerous vs. benign
- Using entropy to determine split point (discretization point)
- Top-down, recursive split
- Details to be covered in "Classification" sessions

Chapter 3: Data Preprocessing

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Summary

Dimensionality Reduction

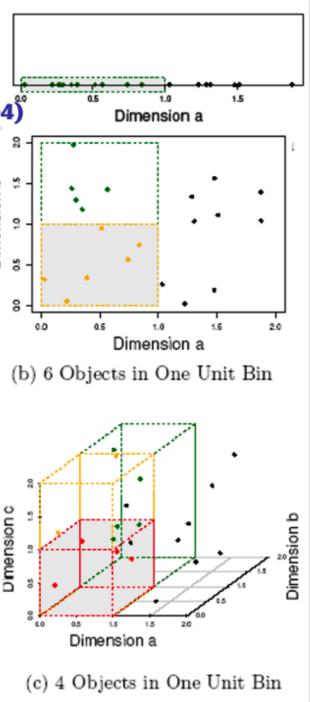
Curse of dimensionality

- When dimensionality increases, data becomes increasingly sparse
- Density and distance between points, which is critical to clustering, outlier analysis, becomes less meaningful
- The possible combinations of subspaces will grow exponentially

The Curse of Dimensionality

(graphs adapted from Parsons et al. KDD Explorations 2004)

- Data in only one dimension is relatively packed
- Adding a dimension "stretch" the points across that dimension, making them further apart
- Adding more dimensions will make the points further apart—high dimensional data is extremely sparse
- Distance measure becomes meaningless—due to equi-distance
 Well, not necessarily. It depends.



Dimensionality Reduction

Curse of dimensionality

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Dimensionality reduction

Reducing the number of random variables under consideration, via obtaining a set of principal variables

Dimensionality Reduction

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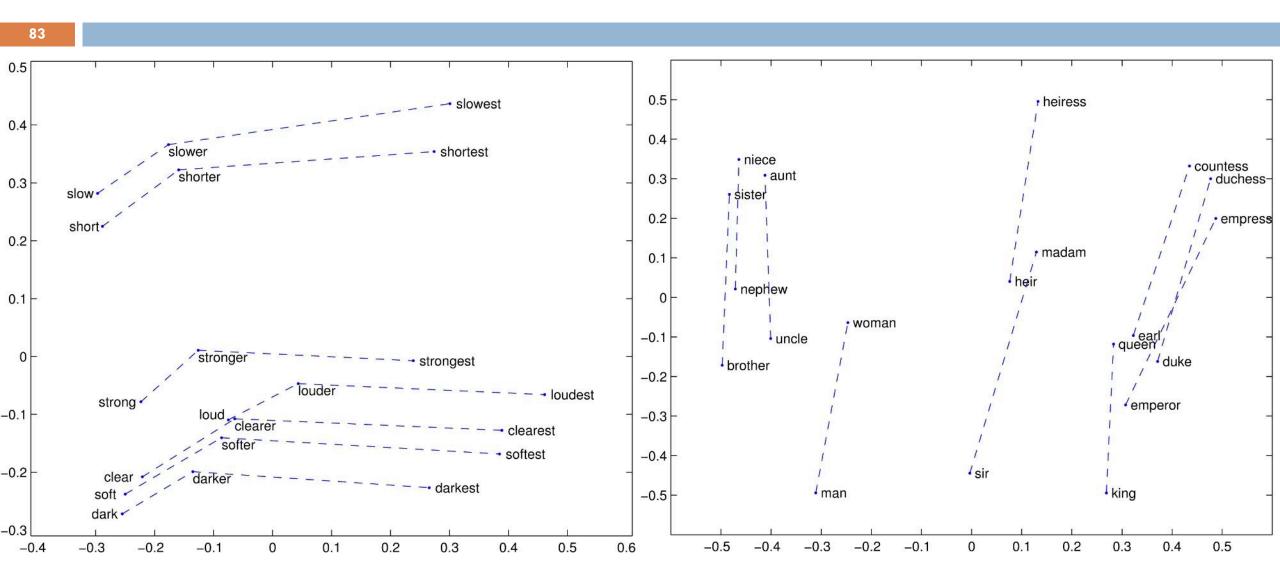
Dimensionality reduction

Reducing the number of random variables under consideration, via obtaining a set of principal variables

Advantages of dimensionality reduction

- Mitigate the curse of dimensionality
- Help eliminate irrelevant features and reduce noise
- Reduce time and space required in data mining
- Allow easier visualization

Word Embedding Visualization via Dim. Reduct.

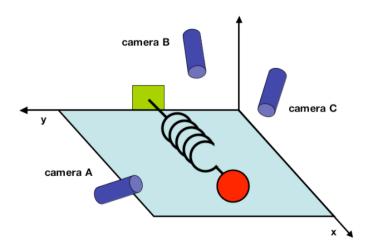


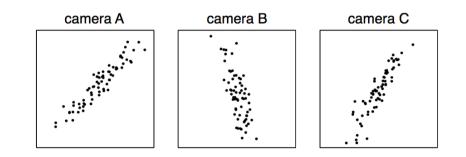
Dimensionality Reduction Techniques

- Dimensionality reduction methodologies
 - **Feature selection**: Find a subset of the original variables (or features, attributes)
 - Feature extraction: Transform the data in the high-dimensional space to a space of fewer dimensions
- Some typical dimensionality reduction methods
 - Principal Component Analysis
 - Supervised and nonlinear techniques
 - Feature subset selection
 - Feature creation

Principal Component Analysis (PCA)

- PCA: A statistical procedure that uses an orthogonal transformation to convert a set of observations of possibly correlated variables into a set of values of linearly uncorrelated variables called principal components
- The original data are projected onto a much smaller space, resulting in dimensionality reduction
- Method: Find the eigenvectors of the covariance matrix, and these eigenvectors define the new space



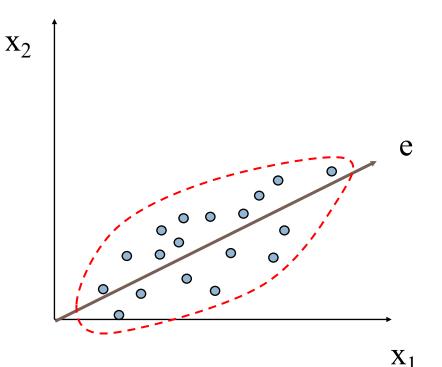


Ball travels in a straight line. Data from three cameras contain much redundancy

Principal Components Analysis: Intuition

Goal is to find a projection that captures the largest amount of variation in data

- □ Find the eigenvectors of the covariance matrix
- □ The eigenvectors define the new space



Principal Component Analysis: Details

Let A be an $n \times n$ matrix representing the covariance of the data. λ is an eigenvalue of A if there exists a non-zero vector v such that: $Av = \lambda v$

In this case, vector *v* is called an eigenvector of A corresponding to λ.
 For each eigenvalue λ, the set of all vectors *v* satisfying Av = λv is called the eigenspace of A corresponding to λ.

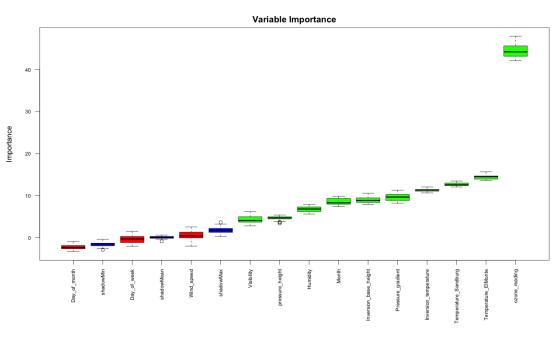
Attribute Subset Selection

□ Another way to reduce dimensionality of data

- Redundant attributes
 - Duplicate much or all of the information contained in one or more other attributes
 - E.g., purchase price of a product and the amount of sales tax paid

Irrelevant attributes

- Contain no information that is useful for the data mining task at hand
 - Ex. A student's ID is often irrelevant to the task of predicting his/her GPA



Heuristic Search in Attribute Selection

- \Box There are 2^d possible attribute combinations of d attributes
- Typical heuristic attribute selection methods:
 - Best single attribute under the attribute independence assumption: choose by significance tests
 - Best step-wise feature selection:
 - The best single-attribute is picked first
 - Then next best attribute conditioned to the first, ...
 - Step-wise attribute elimination:
 - Repeatedly eliminate the worst attribute
 - Best combined attribute selection and elimination
 - Optimal branch and bound:
 - Use attribute elimination and backtracking

Attribute Creation (Feature Generation)

- Create new attributes (features) that can capture the important information in a data set more effectively than the original ones
- Three general methodologies
 - Attribute extraction
 - Domain-specific
 - Mapping data to new space (see: data reduction)
 - E.g., Fourier transformation, wavelet transformation, manifold approaches (not covered)
 - Attribute construction
 - Combining features (see: discriminative frequent patterns in Chapter on "Advanced Classification")
 - Data discretization



- Data quality: accuracy, completeness, consistency, timeliness, interpretability, trustworthiness
- Data cleaning: e.g. missing/noisy values, outliers
- **Data integration** from multiple sources:
 - Entity identification problem; Remove redundancies; Detect inconsistencies

Data reduction

Dimensionality reduction; Numerosity reduction; Data compression

Data transformation and data discretization

Normalization; Concept hierarchy generation

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